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at 500 MB using harmonic analysis of the
height field with its square grid computation

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A COMPARISON OF GEOSTROPHIC RELATIVE
VORTICITY AT 500 MB USING HARMONIC
ANALYSIS OF THE HEIGHT FIELD WITH
ITS SQUARE GRID COMPUTATION

CHI-CHEN CHEN
and
CHARLES E. CANTRELL, JR.

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USING HARMONIC ANALYSIS OF THE HEIGHT FIELD
WITH ITS ~~ITS~~ SQUARE GRID COMPUTATION

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A COMPARISON OF GEOSTROPHIC RELATIVE VORTICITY AT 500 MB
USING HARMONIC ANALYSIS OF THE HEIGHT FIELD
WITH ITS SQUARE GRID COMPUTATION

by

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ABSTRACT

Geostrophic relative vorticity is computed along three latitude circles generally encompassing the United States, using a Fourier analysis of the 500-mb height field for the period 3-6 November 1961.

A statistical comparison of vorticity obtained in this manner with its square grid computation is made.

The writers are deeply indebted to Professor F. L. Martin of the United States Naval Postgraduate School for his suggestion of the topic and his continued help throughout the investigation and during the preparation of this paper.



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LIST OF SYMBOLS USED

Symbol	Definition
f_g	vertical component of geostrophic relative vorticity
g	acceleration due to gravity
f	coriolis parameter
z	contour height
a	radius of earth
Ω	angular velocity of earth
ϕ	latitude
$\Delta\phi$	difference in latitude
λ	longitude
β	$2\Omega \cos \phi / f$
\bar{z}	zonally averaged contour height
z^*	perturbation of zonal contour height
\bar{z}	space-mean contour height
d	grid mesh = 381 km
n	wave number
N	latitude circles numbered 1 through 27 grid lengths from the north pole
C_n	amplitude of <u>n</u> th wave
Θ_n	phase angle of <u>n</u> th wave
m	map factor
r	radius of earth at latitude ϕ , $r = a \cos \phi$
f_{FNWF}	vertical component of geostrophic relative vorticity as computed by Fleet Numerical Weather Facility
F	F test for equality of variances
p	number of predictors (independent variables)
u_g	geostrophically-computed zonal component of the wind
U_g	mean zonal wind computed geostrophically



Symbol	Definition
RMS	root mean square
R	multiple correlation coefficient
n	number of cases in sample

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1. Introduction.

The advent of the electronic computer coupled with increased data coverage has removed the primary obstacles to the use of harmonic analysis as a useful instrument in atmospheric research.

Use is made of a Fourier analysis of the 500-mb height field. A computer program devised by G. Arnason and M. Reese and made available by Fleet Numerical Weather Facility¹ was used to obtain the harmonic analysis around latitude circles at distances of 1 through 27 grid lengths $d = 381$ km from the pole. An equation for relative vorticity using the results of the spherical harmonic analysis is derived and tested statistically against the more usual numerical computation of geostrophic relative vorticity made using a square grid.

The problem undertaken was to compute relative vorticity at 500 mb using the geostrophic vorticity equation in its spherical coordinate form [1, p. 358].

$$\zeta_g = \frac{g}{a} \left(\frac{\partial^2 z}{\partial \lambda^2} + \frac{\partial^2 z}{\partial \phi^2} \right) - \frac{U_g}{a} \tan \phi + \dots \quad (1)$$

In equation (1), z was replaced by its expression in terms of a Fourier analysis

$$Z = \bar{Z} + \sum_{n=1}^M [C_n \sin(n\lambda - \phi_n)] = \bar{Z} + Z^* \quad (2)$$

Here \bar{z} is the zonally averaged contour height, whereas z^* is the perturbation quantity which remains when the \bar{z} field is subtracted from the actual height field. The computer printout included maps of each of these three fields at 500 mb for the period under investigation, 3 through 6 November 1961. Geostrophic relative vorticity was computed by the above mentioned technique for 17 longitudes along each of three latitude circles generally

¹Henceforth referred to as FNUF



encompassing the north-south extent of the United States. This gave a total sample size of 204 computed relative vorticities which were then correlated with square-grid computations of relative vorticities obtained from FNWF charts of absolute vorticity for exactly the same set of points and times.

2. The geostrophic relative vorticity in terms of a harmonically analyzed contour field.

The adequacy of the Fourier representation of meteorological parameters will not be discussed here; the interested reader is referred to [2].

It was previously mentioned that use was made of the FNWF computer program for a Fourier analysis of the 500 mb contour field. A brief description of the theory and numerical evaluation of the Fourier coefficients is given in [3] and only the applicable portions of the program will be mentioned here.

The zonal mean height \tilde{z} is defined as

$$\tilde{z} = \frac{1}{2\pi} \int_0^{2\pi} z \, d\lambda \quad (3)$$

and its zonal perturbation, in accordance with equation (2), is

$$z^* = z - \tilde{z} \quad (4)$$

Expanding z in a Fourier series one obtains at a given latitude

$$z = \tilde{z} + \sum_{n=1}^M [A_n \cos n\lambda + B_n \sin n\lambda] \quad (5)$$

where A_n and B_n are the coefficients of the n th harmonic functions in the Fourier expansion of z , and M is the total number of harmonic waves necessary to resolve the contour field. Replacing A_n and B_n in (5) by an amplitude factor C_n and a phase angle ϕ_n , (5) may be rewritten as

$$\tilde{z} = z^* + \sum_{n=1}^M C_n \sin(n\lambda - \Theta_n) \quad (6)$$

where

$$C_n = \sqrt{A_n^2 + B_n^2} \quad \text{and} \quad \tan \Theta_n = -B_n/A_n$$

Equation (6) has been programmed for the CDC-1604 digital computer by FNNF, and the program includes: a contour grid map of the zonal perturbation field z^* , and a tabular list of the Fourier parameters C_n , Θ_n and \tilde{z} for each of 27 latitude circles. The last three parameters are actually computed in relation to a zonal band of width equal to the grid mesh d of the FNNF map grid, but may be considered applicable at the center of the band.

Using spherical coordinates λ and ϕ (longitude and latitude, respectively) the derivative operators

$$\frac{\partial}{\partial x} = \frac{1}{a \cos \phi} \frac{\partial}{\partial \lambda} \quad \text{and} \quad \frac{\partial}{\partial y} = \frac{1}{a} \frac{\partial}{\partial \phi}$$

apply, and we have

$$\Delta_g = \frac{g}{a^2 f} \left(\frac{1}{\cos \phi} \frac{\partial^2 \tilde{z}}{\partial \lambda^2} + \frac{\partial^2 \tilde{z}}{\partial \phi^2} \right) + \frac{2}{a} \mu_g \csc \phi \quad (7)$$

since

$$\partial/\partial r = \frac{1}{a} \cot \phi$$

If now z is replaced in (7) by its expansion in a Fourier series as given in equation (2) we obtain

$$\Delta_g = \frac{g}{a^2 f} \left\{ \frac{1}{\cos \phi} \frac{\partial^2}{\partial \lambda^2} \left[\sum_{n=1}^M C_n \sin(n\lambda - \Theta_n) \right] + \frac{\partial^2}{\partial \phi^2} \left[\sum_{n=1}^M C_n \sin(n\lambda - \Theta_n) \right] \right\} + \frac{2}{a} \mu_g \csc \phi \quad (8)$$

Remembering that C_n and Θ_n are independent of longitude λ but not of



latitude ϕ , we may perform the indicated differentiations and combine terms, with the result that J_g in spherical coordinates becomes

$$J_g = \frac{g}{f \sin \phi} \left\{ -\frac{1}{\sin \phi} \sum_{n=1}^M \left[n^2 C_n \sin(n\lambda - \Theta_n) \right] + \sum_{n=1}^M \left[\sin(n\lambda - \Theta_n) \left(\frac{\partial^2 C_n}{\partial \phi^2} - C_n \left(\frac{\partial \Theta_n}{\partial \phi} \right)^2 \right) \right] \right. \\ \left. - \sum_{n=1}^M \left[\cos(n\lambda - \Theta_n) \left(C_n \frac{\partial^2 \Theta_n}{\partial \phi^2} + \frac{\partial C_n}{\partial \phi} \frac{\partial \Theta_n}{\partial \phi} \right) \right] \right\} + \frac{g}{f} \mu_g \csc 2\phi \quad (9)$$

Equation (9) may be shown to have the form

$$J_g = \frac{g}{f} \sum_{n=1}^M \left\{ \left[-\frac{n^2}{\sin^2 \phi} + \frac{1}{\sin^2 \phi} \left(\frac{\partial^2 C_n}{\partial \phi^2} - C_n \left(\frac{\partial \Theta_n}{\partial \phi} \right)^2 \right) \right] C_n \sin(n\lambda - \Theta_n) \right. \\ \left. - \frac{g}{f \sin \phi} \frac{1}{n \sin \phi} \left[2 \frac{\partial C_n}{\partial \phi} \frac{\partial \Theta_n}{\partial \phi} + C_n \frac{\partial^2 \Theta_n}{\partial \phi^2} \right] \right\} \sin(n\lambda - \Theta_n) \\ + \mu_g \csc 2\phi. \quad (10)$$

Since

$$Z = \sum_{n=1}^M C_n \sin(n\lambda - \Theta_n) \quad \text{and} \quad \frac{\partial Z}{\partial \lambda} = \sum_{n=1}^M n C_n \cos(n\lambda - \Theta_n),$$

equation (10) may be approximated by

$$J_g = \frac{2\mu_g}{f} \csc 2\phi + \frac{g}{f} \left\{ -\frac{n^2}{\sin^2 \phi} + \frac{1}{\sin^2 \phi} \left[\frac{\partial^2 C_n}{\partial \phi^2} - C_n \left(\frac{\partial \Theta_n}{\partial \phi} \right)^2 \right] \right\} Z \\ - \frac{g}{f \sin \phi} \left\{ \frac{1}{n \sin \phi} \left[2 \frac{\partial C_n}{\partial \phi} \frac{\partial \Theta_n}{\partial \phi} + C_n \frac{\partial^2 \Theta_n}{\partial \phi^2} \right] \right\} \frac{\partial Z}{\partial \lambda} \quad (11)$$

Here the superscript bar denotes an average with respect to n over all significant waves $n = 1, \dots, M$.

The FNWF maps are stereographic maps true at latitude 60°N , and elsewhere the grid mesh, $d = 381$ km, is related to the true distance d_T by the relationship $d = m d_T$, where $m = (1 + \sin 60)/(1 + \sin \phi)$ and is the so-called map factor.

The partial derivatives in (11) may be evaluated by centered finite differences. The numerical values of C_n and Θ_n were simply taken from



the tabular list of computer output of the harmonic analysis at the various latitude circles. For example, $\partial^2 \zeta_n / \partial \phi^2$ may be written using finite differences between adjacent latitude circles (for which $\Delta \phi = d/m$) in the form

$$\frac{1}{d^2} \frac{\partial^2 \zeta_n}{\partial \phi^2} = \frac{\zeta_{N-1,n} - 2\zeta_{N,n} + \zeta_{N+1,n}}{d^2/m^2}.$$

The latitude circles of the Fourier analysis employed in the computation of $\int_0^{\pi} \zeta_n$ corresponded to $N = 12, 15$, and 18 grid mesh distances from the pole, which in turn corresponded to the latitude circles: $48.9N$, $38.6N$, and $28.3N$ (see fig. 1). However, in the computation of first and second derivatives of the n th Fourier wave parameters, these parameters at latitude circles $N-1$ and $N+1$ are also needed.

The term $\partial \zeta^* / \partial \lambda$ is more tractable in the present case if the finite-difference substitution $r(\lambda) = 2d/m$ is made; thus, the centered derivative $\partial \zeta^* / \partial \lambda$ in finite differences, assumes the form

$$\frac{\partial \zeta^*}{\partial \lambda} = \frac{r}{2d} (\zeta_{i+1}^* - \zeta_{i-1}^*) \quad (12)$$

where $r = d \cos \phi$ is the radius of the latitude circle, and the subscript $i+1$ is one grid mesh eastward of the i th point along the latitude circle.

Including the form of $\partial \zeta^* / \partial \lambda$ given in (12), equation (11) may now be written in the more compact form

$$\bar{\zeta}_n = \frac{2}{\pi} W_1 u_n \csc 2\phi + W_1 \zeta_i^* + W_2 (\zeta_{i+1}^* - \zeta_{i-1}^*) \quad (13)$$

where

$$W_1 = \frac{2}{\pi} \left\{ -\frac{n^2}{d^2 \cos^2 \phi} + \frac{1}{d^2} \left[\frac{\partial^2 \zeta_n}{\partial \phi^2} - \zeta_n \left(\frac{\partial^2}{\partial \phi^2} \right) \right] \right\}$$

$$W_2 = -\frac{1}{2 + \pi d} \left[\frac{1}{n \zeta_n} \left(2 \frac{\partial \zeta_n}{\partial \phi} \frac{\partial \zeta_n}{\partial \phi} + \zeta_n \frac{\partial^2 \zeta_n}{\partial \phi^2} \right) \right]$$

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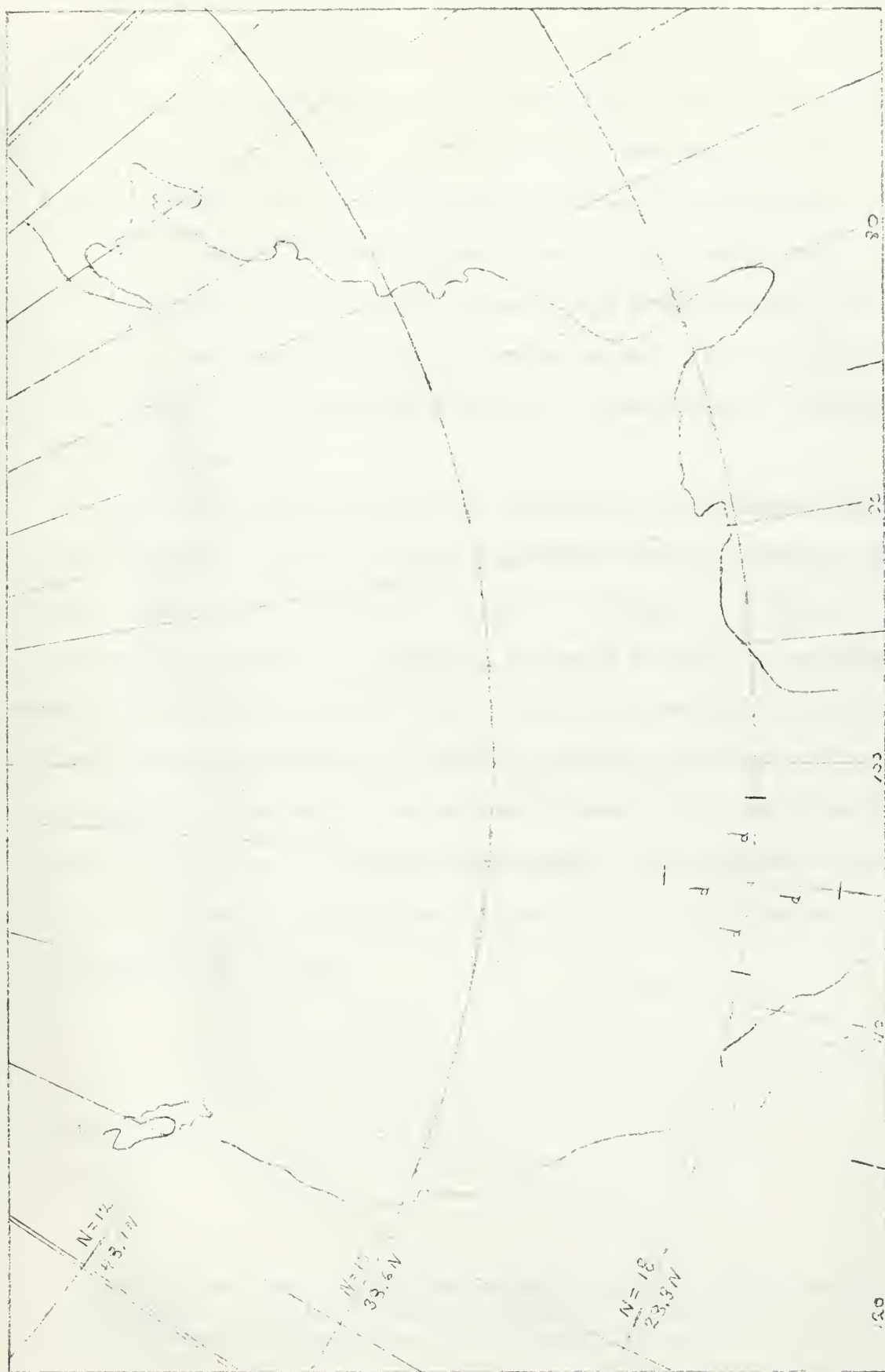


Fig. 1. Grid overlay depicting latitude circles $N=12, 15, 18$ and the grid mesh length d . Geostrophic relative vorticity is computed at the intersections of the latitude circles with all 5° longitude lines lying within the area bounded by the double-line meridians.



The averaging with respect to n in the expressions for W_1 and W_2 is assumed to be valid, according to the mean value theorem. Actually however the average was approximated by a simple arithmetic mean of the contributions for $n = 1, \dots, M$. Thus it was necessary to compute contributions for each n and divide the result by the number of waves.

Van Mieghem [2] points out that waves of space number higher than 12 to 17 contribute little to the variance of the contour-height field. Consequently, the Fourier analysis was truncated at $M = 12$ at the two higher latitude circles,¹ although wave numbers 1 through 15 were employed at the lowest latitude.

The coefficients W_1 and W_2 are constants for a particular time and latitude circle, and can be computed directly from the tabulated harmonic data. These values are listed in table 1. However, in applying equation (13) it was necessary to interpolate values of z^* from the perturbation map at the points indicated in fig. 1 along the specified latitude circles. These points were arbitrarily chosen at integral multiples of five degrees of longitude, encompassing the west-east extent of the United States. Therefore, for ease in selecting data points, a grid overlay was constructed presenting all latitude circles $N=11, \dots, 19$, drawn so as to incorporate the map factor.

¹At the two higher latitudes, W_1 was negative ensuring that lows corresponded to positive relative vorticity. At the lowest latitude ($N=18$), it was necessary to use $M=15$ in order to ensure that this condition was met.

The first part of the paper discusses the importance of the study and the objectives of the research. It also provides a brief overview of the methodology used in the study. The second part of the paper presents the results of the study and discusses the implications of the findings. The third part of the paper concludes the study and provides some final thoughts on the research.

The study was conducted using a qualitative research approach. The data was collected through interviews with participants who were selected through purposive sampling. The interviews were conducted in a semi-structured format, allowing the researcher to explore the topics in depth while also following a general guide. The data was then analyzed using thematic analysis, which involves identifying themes or patterns in the data.

The findings of the study suggest that there are several factors that influence the outcomes of the research. These factors include the quality of the data, the reliability of the participants, and the effectiveness of the research methods. The study also found that there are some limitations to the research, such as the small sample size and the potential for bias.

In conclusion, the study provides valuable insights into the research process and the importance of using appropriate methods and participants. The findings suggest that there are several factors that influence the outcomes of the research, and that there are some limitations to the research. The study also provides some final thoughts on the research.

TABLE 1: Values of W_1 and W_2 to be applied in equation (1). All values are in units of $10^{-6} \text{ sec}^{-1} \text{ ft}^{-1}$.

DATE	LATITUDE CIRCLE		
	N = 12	N = 15	N = 18
3 Nov. 1961	$W = -.1467$	$W = -.1635$	$W = -.2696$
	$W = -.0079$	$W = -.0370$	$W = -.0303$
4 Nov. 1961	$W = -.1490$	$W = -.0617$	$W = -.0420$
	$W = -.0311$	$W = .0316$	$W = .0138$
5 Nov. 1961	$W = -.1355$	$W = -.1013$	$W = -.1819$
	$W = -.0398$	$W = -.0230$	$W = .1682$
6 Nov. 1961	$W = -.0551$	$W = -.1460$	$W = -.3510$
	$W = .0757$	$W = .0349$	$W = -.7610$

Note that the term $(2u_z + 2\phi)/\Delta$ in both (11) and (13) also varies from point to point around any latitude circle. However, the variation of this term was so small that the mean zonal wind for the latitude was used. The mean zonal wind U_z was computed using the latitudinal gradient of zonal mean height \bar{z} , that is from

$$U_z = \frac{1}{\Delta} \frac{\partial \bar{z}}{\partial \phi} \quad ,$$

again using finite differences.

Along each of the three latitude circles, 17 values of $W_1 z^*$ and $W(z_{i+1}^* - z_{i-1}^*)$ were obtained for each of the four days, giving a total of 204 separate values of these quantities.

3. Statistical results.

For precisely the same set of points and days as described above, corresponding values of \bar{f}_2 were obtained from grid maps of geostrophic relative vorticity made available by FNMF. Their maps essentially presented the field of \bar{f}_2 computed using their square-grid mesh according

to the usual formula

$$\int_{FNWF} = \frac{4\pi m^2}{j^2} (\bar{z} - t), \quad (14)$$

where \bar{z} is the four-point space-mean contour height and $d = 381$ km at latitude 60N.

Since the averaging process in equation (11) is somewhat approximate, it was felt that better verification would result if the relationship between \int_{FNWF} and $W_1 z_L^*$ and $W_2 (z_{L+1}^* - z_{L-1}^*)$ was written

$$\int_{FNWF} = \frac{2}{9} (1) g \cos \phi + A_0 + A_1 (W_1 z_L^*) + A_2 [W_2 (z_{L+1}^* - z_{L-1}^*)] \quad (15)$$

Here A_0 , A_1 , and A_2 are regression coefficients¹ to be determined by a least squares technique applied to the 204 simultaneous values of $W_1 z_L^*$ and $W_2 (z_{L+1}^* - z_{L-1}^*)$. Because of occasional large gradients of \int_{FNWF} over 5° longitude intervals, the values of \int_{FNWF} were smoothed by the three-point binomial running mean formula

$$\bar{X}_L = (X_{L-1} + 2X_L + X_{L+1}) / 4$$

where X_L is any value of \int_{FNWF} interpolated from the FNWF vorticity-grid map at each point. The regression equation actually involves the correlation of the smoothed $\bar{\int}_{FNWF}$ values with the independent variables already noted.

Using the BMD 06 statistical program as adapted to the CDC-1604 computer, it was necessary to type 204 IBM cards containing the smoothed $\bar{\int}_{FNWF}$ values and the simultaneous values of the independent variables of the right side of equation (15). Best-fitting values of the regression coefficients were

¹These regression coefficients are non-dimensional since the units of $W_1 z_L^*$ and $W_2 (z_{L+1}^* - z_{L-1}^*)$ are in sec^{-1} .

The first part of the document discusses the importance of maintaining accurate records of all transactions. It emphasizes that proper record-keeping is essential for the company's financial health and for providing reliable information to stakeholders. The document also outlines the specific procedures for recording transactions, including the use of standardized forms and the requirement for double-checking entries.

In addition to record-keeping, the document highlights the need for regular audits to ensure the accuracy and integrity of the financial data. It states that audits should be conducted at least once a year by an independent third party. The document also provides guidance on how to handle discrepancies and how to resolve any issues that may arise during the audit process.

The document further discusses the importance of transparency and communication in financial reporting. It encourages the company to provide clear and concise reports to its shareholders and to be open to questions and feedback. The document also outlines the specific requirements for financial reporting, including the use of standardized formats and the inclusion of all relevant information.

Finally, the document concludes by reiterating the company's commitment to financial integrity and transparency. It states that the company will continue to strive for excellence in all aspects of its financial reporting and that it will always be open to suggestions and improvements. The document also provides a list of resources and contacts for further information.

$$A_0 = -8.1719,$$

$$A_1 = 0.4585,$$

$$\text{and } A_2 = 0.0624$$

The standard error of estimate¹ and the multiple linear correlation coefficient for the regression equation were 20.3523 and 0.7632 respectively.

Panofsky and Brier [4, p. 113] present an F test for the analysis of the variance explained by the regression equation. The F value may be defined by the ratio of the explained variance to the residual variance relative to the regression equation. This formula is

$$F = \frac{R^2 (n-p-1)}{(1-R^2) p} \quad (16)$$

With $p = 2$, the number of independent variables, and $n = 204$, the number of random samples, the value of F from equation (16) turns out to be 139.33. However, assuming normally distributed independent and dependent variables, the critical F at the 0.99 significance level with 2 and 201 degrees of freedom is 4.71. Thus the regression equation (15) is significant at a very high confidence level.

The partial correlation coefficients of $W_1 z_L^*$ and $W_2 (z_{L+1}^* - z_{L-1}^*)$ were 0.7620 and 0.0382, respectively, indicating very little contribution to the regression equation for the latter variable. An intuitive explanation for the insignificant contribution of $W_2 (z_{L+1}^* - z_{L-1}^*)$ may be obtained from fig. 2. The differences, $z_{L+1}^* - z_{L-1}^*$, taken over the pressure centers would be zero, whereas in actuality the largest absolute values of \dot{f}_y would be found at these points. Likewise for a sinusoidal contour wave pattern maximum magnitudes of $z_{L+1}^* - z_{L-1}^*$ would exist near contour inflection points, where $\dot{f}_y \approx 0$.

The possibility of "automatic" correlation, viz, correlation between the two independent variables, was examined and none was found to exist.

¹All values of \dot{f}_y are in units $\times 10^{-6} \text{ sec}^{-1}$.

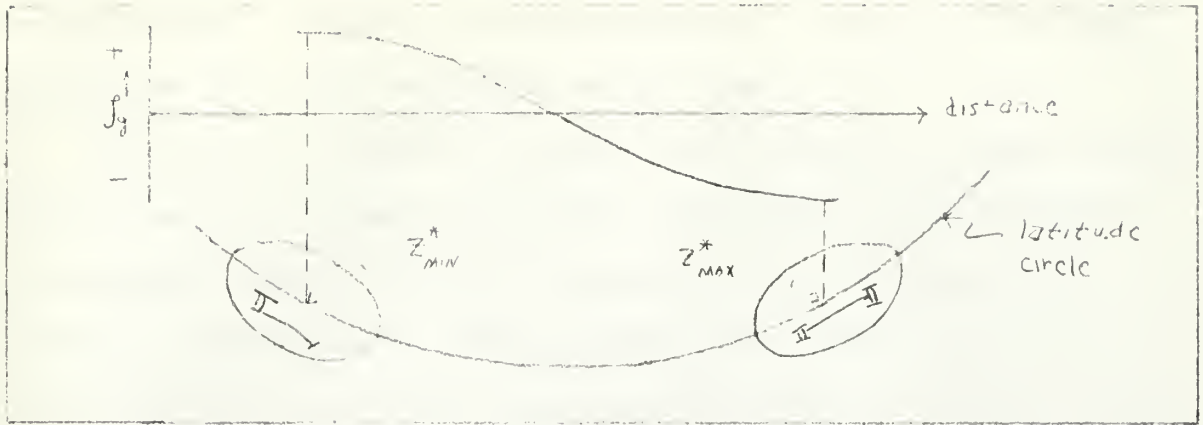


Fig. 2. Distribution of J_g along a latitude circle between contour maximum and minimum, in the case of a sinusoidal contour wave.

The individual latitude circles were statistically examined in a like manner. The two northernmost latitude circles gave a multiple linear correlation coefficient of 0.84, whereas there is no significant correlation between J_{PNWF} and the two independent variables $W_1 z_L^*$ and $W_2 (z_{L+1}^* - z_{L-1}^*)$ at latitude 28.3N. This inconsistency at low latitudes is attributable to "noise" in the Fourier representation of the contour field. The "noise" is due to the small variance of the height field at this latitude, coupled with the relatively large RMS error possible in the 500 mb analysis in the subtropics during the period of study. The use of second derivatives of the Fourier parameters also increases the amount of "noise" generated in the determination of J_g .

4. Conclusions.

Theoretically there should have been a large positive multiple linear correlation between J_{PNWF} and $W_1 z_L^*$ and $W_2 (z_{L+1}^* - z_{L-1}^*)$. This proved to be the case at latitudes 48.9N and 38.6N where the contour field was well resolved by twelve harmonic waves. However, at the lowest latitude circle, 28.3N, the several sources of errors listed at the end of section 3 could, and probably did, influence the low correlations that were obtained. These were basically due to the lack of resolution of the contour field by the

Fourier analysis. However, the same reasons would cause the square-grid computation of $\int q$ to be subject to large errors.

Based upon the results at the two higher latitudes, it seems apparent that the use of a Fourier analysis of a meteorological field presents a very valuable tool for atmospheric research. With the advent of the electronic computer and machine-analyzed contour charts, the use of harmonic analysis is an effective and economically feasible approach to the computation of synoptic aids for the practising meteorologist.

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